

## Structure and Magnetic Properties of $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ : a New Copper Borate Featuring $[\text{Cu}_3\text{O}_8]^{10-}$ Units

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$\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  crystallizes in the monoclinic space group  $P2/n$  (No. 13) with  $a = 6.8016(15)$  Å,  $b = 4.7123(10)$  Å,  $c = 14.614(3)$  Å,  $\beta = 97.089(3)^\circ$ , and  $Z = 2$ . The crystal structure consists of infinite  $[\text{Cu}_3\text{O}_8]^{10-}$  zigzag chains of alternating dimers and monomers. The magnetic susceptibility and specific heat capacity show spin-gap and Curie–Weiss behaviors that can be explained by a model of  $\text{Cu}(2)$ – $\text{Cu}(2)$  dimers and isolated or weakly coupled  $\text{Cu}(1)$  monomers.

### Introduction

Mixed-metal oxides that contain copper dimers or trimers have received considerable attention, owing to their interesting magnetic properties.<sup>1–10</sup> For example,  $\text{La}_4\text{Cu}_3\text{MoO}_{12}$  is an isolated Heisenberg triangle spin trimer model,<sup>2,3</sup> in which the antiferromagnetic intratrimer interactions are frustrated.  $\text{A}_3\text{Cu}_3(\text{PO}_4)_4$  with  $\text{A} = \text{Ca}, \text{Sr}, \text{or Pb}$  is a model system of the linear Heisenberg antiferromagnetic  $S = 1/2$  trimer.<sup>4</sup>  $\text{SrCu}_2(\text{BO}_3)_2$  is a model system of isolated spin dimers.<sup>8</sup>

These phases display unique spin interactions and spin exchange pathways.

The exchange pathways in extended structures can be complex, and it is important to understand these pathways for device applications. Understanding spin exchange dynamics contributes to the basic knowledge of chemical bonds, which in turn leads to new and improved materials, for example, nanoscale materials for magnetic memory.

An extensive search of the  $\text{PbO}$ – $\text{CuO}$ – $\text{B}_2\text{O}_3$  system has led to a new phase,  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ . In the current work, the interesting magnetic properties are reported and current models are adapted to discuss the spin exchange interactions. The synthesis, crystal structure, vibrational spectroscopy, magnetic susceptibility, and specific heat capacity of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  are reported.

### Experimental Section

**Synthesis.** Polycrystalline  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  was prepared in a platinum crucible by solid-state reaction method using stoichiometric ratios of  $\text{PbO}$  (99.99%, Alfa-Aesar),  $\text{CuO}$  (99.995%, Alfa-Aesar), and  $\text{B}_2\text{O}_3$  (99.98%, Sigma-Aldrich). The mixture was heated slowly from room temperature to 600 °C in air for 2–3 days with intermittent grinding. The sample purity was verified using X-ray powder diffraction.

X-ray powder diffraction analysis of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  was performed at room temperature in the angular range of  $2\theta = 10$ – $70^\circ$  with a scan step width of  $0.02^\circ$  and a fixed counting time of 1 s/step using an automated Rigaku X-ray diffractometer equipped with a diffracted-beamed monochromator set for  $\text{Cu K}\alpha$  ( $\lambda = 1.5418$  Å) radiation. The experimental powder X-ray diffraction pattern of  $\text{Pb}_2$

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Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub> is in agreement with the calculated data based on the single-crystal data, suggesting that it is pure phase (Figures S1 and S2 in the Supporting Information).

**Crystal Growth.** A covered platinum crucible containing a 1:1:1 molar ratio of PbO, CuO, and B<sub>2</sub>O<sub>3</sub> was placed into the center of a vertical, programmable temperature Molybdenum furnace. The furnace was heated to a temperature of 970 °C at a rate of 10 °C/min, maintained for 24 h, cooled to 600 °C at a rate of 0.1 °C/min, and finally cooled to room temperature at a rate of 10 °C/min. Blue platelike crystals were separated from the melt for the structure determination.

**X-ray Crystallographic Studies.** A plate-shaped blue single crystal of Pb<sub>2</sub>Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub> with the dimensions 0.01 × 0.13 × 0.60 mm<sup>3</sup> was chosen for the structure determination. Unit cell parameters were derived from a least-squares analysis of 3124 reflections in the range 3.48° < θ < 29.03° on a Bruker SMART – 1000 CCD diffractometer using monochromatic Mo Kα radiation (λ = 0.71073 Å) and integrated with the SAINT-Plus program.<sup>11</sup>

All calculations were performed with programs from the SHELXTL crystallographic software package.<sup>12</sup> The space group *P2<sub>1</sub>/n* was determined unambiguously from the systematic absences, and the structure was solved by direct methods. A face-indexed absorption correction was performed using the XPREP program, followed by the SADABS program;<sup>13</sup> equivalent reflections were then averaged. Final least-squares refinement on *F*<sub>0</sub><sup>2</sup> with data having *F*<sub>0</sub><sup>2</sup> ≥ 2σ(*F*<sub>0</sub><sup>2</sup>) includes anisotropic displacement parameters for all atomic positions. The final difference Fourier synthesis may have shown maximum and minimum peaks at 4.165 (0.85 Å from Pb<sub>1</sub>) and −4.045 e/Å<sup>3</sup> (0.81 Å from Pb<sub>1</sub>), respectively. Additional crystal data and structure refinement information are summarized in Table 1.

**Vibrational Spectroscopy.** The mid-infrared spectrum was obtained at room temperature via a Bio-Rad FTS-60 FTIR spectrometer. The sample was mixed thoroughly with dried KBr (5 mg of the sample, 500 mg of KBr), and the spectrum was collected in a range from 400 to 4000 cm<sup>−1</sup> with a resolution of 2 cm<sup>−1</sup>.

**Differential Thermal Analysis.** Differential thermal analysis (DTA) was performed under static air on a TA Instruments, Inc. differential thermal analyzer 1600-2910 DSC. The sample and reference (Al<sub>2</sub>O<sub>3</sub>) were enclosed in Pt crucibles, heated from room temperature to 970 °C, and then cooled to room temperature at a rate of 10 °C/min.

**Magnetic and Specific Heat Measurements.** Direct current (dc) magnetic susceptibility (χ = *M*/*H*) was measured on a Quantum Design MPMS5 Superconducting Quantum Interference Device (SQUID) magnetometer in the temperature ranges 2–300 and 4–400 K in an applied field of 500 Oe under both zero-field-cooled (ZFC) and field-cooled (FC) conditions. Specific heat capacity, *C<sub>p</sub>*, versus temperature, *T*, of Pb<sub>2</sub>Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub> was recorded between 2 and 300 K at zero magnetic field and at 9 T by a pulse relaxation method using a Quantum Design PPMS calorimeter.

## Results and Discussion

**Crystal Structure.** Final atomic coordinates and equivalent isotropic displacement parameters are listed in Table 2, and selected interatomic distances and angles are given in Table S1 in the Supporting Information.

**Table 1.** Crystal Data and Structure Refinement for Pb<sub>2</sub>Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub>

empirical formula	Pb <sub>2</sub> Cu <sub>3</sub> B <sub>4</sub> O <sub>11</sub>
temperature	153(2) K
wavelength	0.71073 Å
formula weight	824.24
crystal system	monoclinic
space group	<i>P2<sub>1</sub>/n</i>
unit cell dimens	<i>a</i> = 6.8016(15) Å <i>α</i> = 90° <i>b</i> = 4.7123(10) Å <i>β</i> = 97.089(3)° <i>c</i> = 14.614(3) Å <i>γ</i> = 90°
volume	464.82(17) Å <sup>3</sup>
<i>Z</i>	2
density (calcd)	5.889 g/cm <sup>3</sup>
absorption coefficient	42.908 /mm
<i>F</i> (000)	718
cryst size	0.01 × 0.13 × 0.60 mm <sup>3</sup>
θ range for data collection	3.48–29.03°
index ranges	−8 ≤ <i>h</i> ≤ 9 −6 ≤ <i>k</i> ≤ 6 −19 ≤ <i>l</i> ≤ 18
reflns collected	3645
independent reflns	1124 [ <i>R</i> (int) = 0.0400]
completeness to θ = 29.03	89.7%
max and min transmission	0.64373 and 0.01355
refinement method	full-matrix least-squares on <i>F</i> <sup>2</sup>
data/restraints/params	1124/0/94
GOF on <i>F</i> <sup>2</sup>	1.120
final <i>R</i> indices [ <i>I</i> > 2σ( <i>I</i> )] <sup>a</sup>	<i>R</i> 1 = 0.0345, <i>wR</i> 2 = 0.0940
<i>R</i> indices (all data) <sup>a</sup>	<i>R</i> 1 = 0.0386, <i>wR</i> 2 = 0.0965
extinction coefficient	0.0018(5)
largest diff. peak and hole	4.165 and −4.045 e/Å <sup>3</sup>

<sup>a</sup> *R*1 = Σ||*F*<sub>o</sub>| − |*F*<sub>c</sub>||/Σ|*F*<sub>o</sub>| and *wR*2 = [Σ*w*(*F*<sub>o</sub><sup>2</sup> − *F*<sub>c</sub><sup>2</sup>)<sup>2</sup>/Σ*wF*<sub>o</sub><sup>4</sup>]<sup>1/2</sup> for *F*<sub>o</sub><sup>2</sup> > 2σ(*F*<sub>o</sub><sup>2</sup>) and *w*<sup>−1</sup> = σ<sup>2</sup>(*F*<sub>o</sub><sup>2</sup>) + (0.0651*P*)<sup>2</sup> + 0.1985*P* where *P* = (*F*<sub>o</sub><sup>2</sup> + 2*F*<sub>c</sub><sup>2</sup>)/3.

**Table 2.** Atomic Coordinates (×10<sup>4</sup>) and Equivalent Isotropic Displacement Parameters (Å<sup>2</sup> × 10<sup>3</sup>) for Pb<sub>2</sub>Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub><sup>a</sup>

atom	Wyckoff position	x	y	z	U <sub>eq</sub>
Pb(1)	4 <i>g</i>	−156(1)	4288(1)	6913(1)	8(1)
Cu(1)	2 <i>d</i>	0	0	5000	7(1)
Cu(2)	4 <i>g</i>	3493(2)	4815(2)	5586(1)	7(1)
B(1)	4 <i>g</i>	−3677(17)	−510(19)	5945(8)	8(2)
B(2)	4 <i>g</i>	2957(15)	9980(20)	6604(7)	8(2)
O(1)	4 <i>g</i>	−1880(12)	757(13)	5874(5)	14(2)
O(2)	2 <i>f</i>	2500	1236(18)	7500	8(2)
O(3)	4 <i>g</i>	1784(9)	1856(12)	5913(4)	8(1)
O(4)	4 <i>g</i>	2482(10)	7058(12)	6487(5)	13(1)
O(5)	4 <i>g</i>	−4896(11)	631(11)	6574(5)	9(1)
O(6)	4 <i>g</i>	5724(9)	7090(12)	5479(4)	10(1)

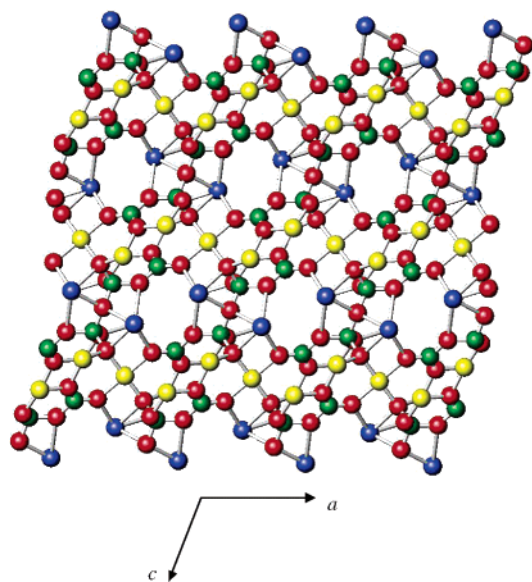
<sup>a</sup> *U*<sub>eq</sub> is defined as one-third of the trace of the orthogonalized *U*<sub>ij</sub> tensor.

The structure of Pb<sub>2</sub>Cu<sub>3</sub>B<sub>4</sub>O<sub>11</sub> is depicted in Figure 1. There is one unique lead site, two unique copper sites, two unique boron sites, and six unique oxygen sites in the asymmetric unit (see Table 2). The coordination of lead is a distorted PbO<sub>5</sub> square pyramid. The oxygen atoms fall within the same hemisphere around lead, owing to the 6s<sup>2</sup> lone electron pair of Pb<sup>2+</sup> in the opposite direction (see Figure 1). The coordination environment around the PbO<sub>5</sub> structure unit is shown in Figure S3 in the Supporting Information. PbO<sub>5</sub> units are surrounded by three separate BO<sub>4</sub> tetrahedra and two separate BO<sub>3</sub> trigonal planar groups. The PbO<sub>5</sub> polyhedron shares edges with four different atoms (Cu(1), Cu(2), B(2) (twice)). The lead atom shares two oxygen atoms (edges) with both Cu(1) and Cu(2) with O(3) common to the Pb(1)O<sub>5</sub>, Cu(1)O<sub>4</sub>, and Cu(2)O<sub>4</sub> polyhedra. Additionally, Pb(1) shares edges with B(2) in two distinct ways. Pb(1)O<sub>5</sub>

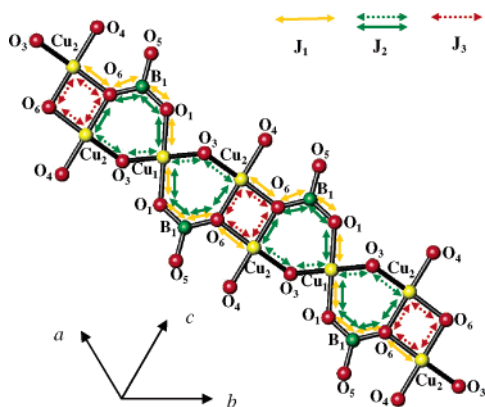
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**Figure 1.** Structure of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ . The blue spheres are Pb, the yellow spheres are Cu, the green spheres are B, the red spheres are O. Lead and boron polyhedra are separated by chains of  $\text{CuO}_4$  polyhedra.

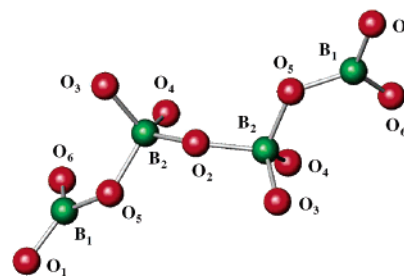


**Figure 2.** Connectivity of the  $\text{CuO}_4$  polyhedra. The yellow spheres are Cu, the red spheres are O, and the green spheres are B. Infinite zigzag chains are formed by  $[\text{Cu}_3\text{O}_8]^{10-}$  units. The  $J_1$ ,  $J_2$ , and  $J_3$  interactions are shown.

is linked to  $\text{B}(2)\text{O}_4$  by both  $\text{O}(3)$  and  $\text{O}(2)$  forming one edge, as well as by  $\text{O}(5)$  and  $\text{O}(2)$  forming the other edge.

The copper atoms exhibit two distinct coordination  $\text{CuO}_4$  polyhedra.  $\text{Cu}(1)$  is surrounded by four oxygen atoms forming a regular rectangular plane, while  $\text{Cu}(2)$  has a slightly distorted rectangular coordination. Important for understanding the magnetic spin interactions, which are discussed later, are the infinite zigzag chains of  $[\text{Cu}_3\text{O}_8]^{10-}$  units that are shown in Figure 2. The chains can be viewed as  $\text{Cu}(2)\text{--Cu}(2)$  dimers that share  $\text{O}(3)$  atoms as corners with  $\text{Cu}(1)$  monomers. Alternatively, the chains can be viewed as  $\text{Cu}_3\text{O}_8$  trimers, where the  $\text{Cu}(1)\text{O}_4$  rectangular plane is linked by  $\text{O}(3)$  on each side by  $\text{Cu}(2)\text{O}_4$  polyhedra.

The boron atoms also exhibit two distinct coordination polyhedra.  $\text{B}(1)$  shows a trigonal planar oxygen coordination, while  $\text{B}(2)$  forms a  $\text{BO}_4$  tetrahedron. The connectivity of the boron–oxygen polyhedra is shown in Figure 3. Corner-sharing  $\text{BO}_4$  dimers are bordered by  $\text{BO}_3$  trigonal planar groups and together form discrete  $\text{B}_4\text{O}_{11}$  tetramers.



**Figure 3.** Connectivity of boron–oxygen polyhedra. The green spheres are B, the red spheres are O. Corner-sharing  $\text{BO}_4$  dimers are bordered by  $\text{BO}_3$  trigonal planar groups, forming isolated  $\text{B}_4\text{O}_{11}$  tetramers.

The bond valence sums of each atom in  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  were calculated<sup>14,15</sup> and are listed in Table 3. These charges, based on the bond lengths determined by the X-ray structure analysis, are in agreement with the expected oxidation states.

**Vibrational Spectroscopy.** IR spectroscopy was carried out with the objective of specifying and comparing the coordination of boron in  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ , and the spectrum from 400 to  $4000\text{ cm}^{-1}$  is shown in Figure S4 in the Supporting Information. The absorptions in IR spectrum of the synthetic sample were assigned on the basis of results obtained from vibrational spectra measurements of other borate groups.<sup>16–19</sup> The main infrared absorption region between about 1200 and  $1400\text{ cm}^{-1}$  reveals two absorption bands, owing to stretching of trigonal  $\text{BO}_3$  ( $1239\text{ cm}^{-1}$ ) and tetrahedral  $\text{BO}_4$  ( $1279\text{ cm}^{-1}$ ) groups, respectively. The bands at 1025, 876, 821, and  $779\text{ cm}^{-1}$  are likely the asymmetric and symmetric stretching of B–O in  $\text{BO}_4$ . In the long-wavelength part of the spectrum there are weak bands at 466, 590, and  $659\text{ cm}^{-1}$  which correspond to the deformation vibrations of the atoms in boron–oxygen polyhedra. The remaining bands in the spectrum are likely attributed to Cu–O and Pb–O vibrations.

**Thermal Stability.** The DTA curve of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  is shown in Figure S5 in the Supporting Information. The sample began to decompose at  $671\text{ }^\circ\text{C}$ , and further decomposition occurs at  $818\text{ }^\circ\text{C}$ , suggesting that  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  melts incongruently. In order to further verify that  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  melts incongruently, 0.8 g of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  powder was heated to  $970\text{ }^\circ\text{C}$  and cooled to room temperature. Analysis of the powder XRD pattern of the melt revealed that the diffraction pattern is different from that of the initial  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  powder (Figure S6 in the Supporting Information), which further suggests that  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  is an incongruently melting compound.

**Magnetic Susceptibility.** Two interpretations of the spin exchange paths in  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  are presented. The first interpretation views the  $[\text{Cu}_3\text{O}_8]^{10-}$  unit as a dimer and a monomer and is presented in the text. The second interpretation views the  $[\text{Cu}_3\text{O}_8]^{10-}$  unit as a trimer and is presented in the Supporting Information. The dimer and monomer model fits the data well numerically and conceptually. The

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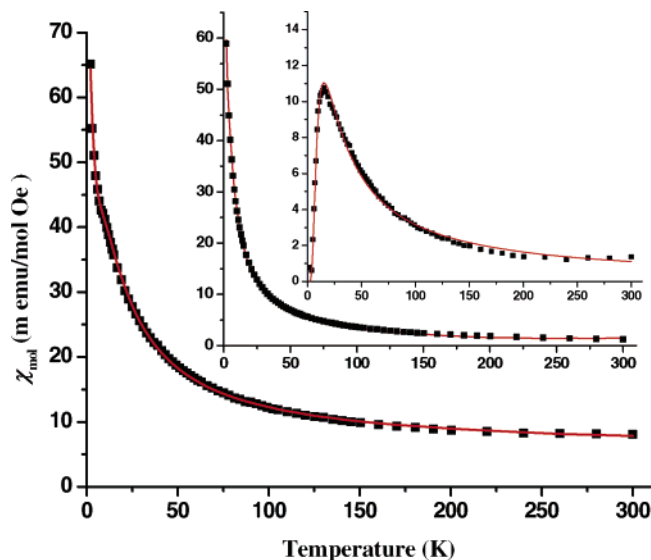


**Table 3.** Bond Valence Analysis of the  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ <sup>a,b</sup>

atom	O(1)	O(2)	O(3)	O(4)	O(5)	O(6)	$\Sigma_{\text{cations}}$
Pb(1)	0.400	[ <sup>×2</sup> ]0.479	0.485	0.506	0.156		2.026
Cu(1)	0.482[ <sup>×2</sup> ]		0.547[ <sup>×2</sup> ]				2.058
Cu(2)			0.531	0.575		0.581 + 0.510	2.197
B(1)	0.987				0.881	1.041	2.909
B(2)		[ <sup>×2</sup> ]0.700	0.715	0.874	0.709		2.998
$\Sigma_{\text{anions}}$	1.869	2.358	2.278	1.955	1.746	2.132	

<sup>a</sup> Bond valences calculated with the program Bond Valence Calculator Version 2.00, Hormillosa, C., Healy, S., Stephen, T. McMaster University (1993).

<sup>b</sup> Valence sums calculated with the formula:  $S_i = \exp[(R_0 - R_i)/B]$ , where  $S_i$  = valence of bond "i" and  $B = 0.37$ . Left and right superscripts indicate the number of equivalent bonds for anions and cations, respectively.



**Figure 4.** Spin-dimer plus monomer model of magnetic response for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ . The bottom graph shows the combined fit, the middle graph shows the Curie–Weiss fit, and the top graph shows the dimer fit.

trimer model also numerically fits the low-temperature anomaly in susceptibility, better than the dimer-plus-monomer model, but provides no cause for the observed large paramagnetic background.

As mentioned above, the crystal structure consists of infinite  $[\text{Cu}_3\text{O}_8]^{10-}$  zigzag chains of alternating dimers and monomers linked by oxygen superexchange paths and oxygen–boron–oxygen super-superexchange paths.  $J_1$  and  $J_2$  in Figure 2 are the interactions between dimer and monomer;  $J_3$  in Figure 2 is the intradimer interaction and is responsible for the spin gap ( $\Delta$ ).

The bottom curve in Figure 4 depicts the  $\chi_{\text{mol}}$  vs  $T$  curve for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ . The magnetic susceptibility curve deviates from the standard Curie–Weiss behavior in the range  $7 \text{ K} < T < 50 \text{ K}$ , implying the formation of a spin gap. The spin-gap hypothesis is supported by the fact that the magnetic susceptibility curve shows a shoulder around 12 K. Spin-gap behavior is plausible in this compound because  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  has a  $\text{Cu}(2)$ – $\text{Cu}(2)$  dimer ( $J_3$  in Figure 2) similar to that in  $\text{SrCu}_2(\text{BO}_3)_2$ , which is an orthogonal dimer system with a spin-gap ground state.<sup>8,20,21</sup> Since  $J_3$  is the intradimer

interaction and the copper atoms of the dimer are in close proximity,  $J_3$  is likely to be dominant. A spin-gap ground state owing to an antiferromagnetic  $J_3$  can then cause the anomaly in the magnetic susceptibility at 12 K while the  $\text{Cu}(1)$  monomer causes the Curie–Weiss response. If  $J_3$  dominates  $J_1$  and  $J_2$  in  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ , the infinite chain can be considered as  $\text{Cu}(2)$ – $\text{Cu}(2)$  dimers and isolated or weakly coupled  $\text{Cu}(1)$  monomers. Because this is a reasonable possibility, the susceptibility data were modeled by chains of alternating dimers and monomers:<sup>8,20,21</sup>

$$\chi = \chi_0 + \frac{N_A \mu_B^2}{k_B} \left[ \frac{g_M^2 S(S+1)}{3(T-\theta)} + \frac{g_D^2}{T(3 + \exp(\Delta/T))} \right] \quad (1)$$

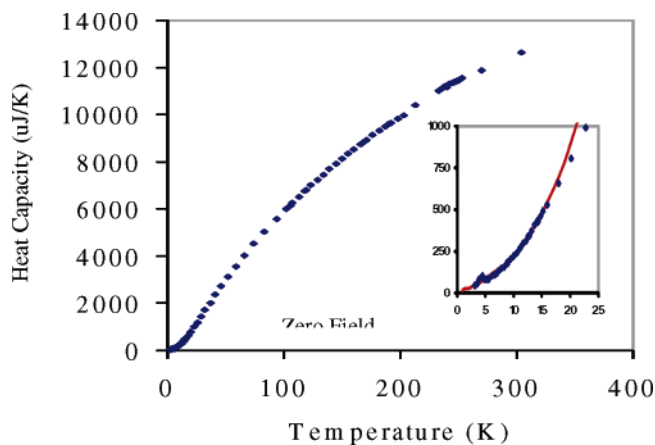
where  $\chi_0$  gives the temperature-independent term;  $g_M$ ,  $g_D$ ,  $N_A$ ,  $\mu_B$ , and  $k_B$  are monomer  $g$ -factor, dimer  $g$ -factor, Avogadro's number, the Bohr magneton, and Boltzmann constant, respectively. The first bracketed term gives the Curie–Weiss response of the monomers (with spin  $S = 1/2$ ), and the last term gives the spin-gap ( $\Delta$ ) response of the dimers. The magnetic susceptibility as a function of temperature can be fit well by this model, and the deviations are similar to those observed by others.<sup>8,20,21</sup> The curve fitting is shown in Figure 4. The best-fit gives  $g_M = 2.01$ ,  $g_D = 1.90$ ,  $\chi_0 = 5.47 \times 10^{-3} \text{ emu/mol}\cdot\text{K}$ ,  $\theta = -4.4 \text{ K}$ ,  $\Delta/k_B = 24.6 \text{ K}$ . The critical temperature in the Curie–Weiss law ( $\theta = -4.4 \text{ K}$ ) agrees well with the transition in the heat capacity discussed later, which is ascribed to magnetic impurities and/or defects on  $\text{Cu}^{2+}$  sites in  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$ .

The bottom curve in Figure 4 represents the original susceptibility data (squares) and the best fit to eq 1 (line). Similarly, the middle curve is the Curie–Weiss portion of the data and the monomer fit and the top curve is the spin-gap data and the dimer fit. The values of data (squares) for the monomer (middle) and dimer (top) contributions were obtained by subtraction from the original susceptibility and were computed and are plotted as the lines in the graphs. The spin gap is evident from the vanishing of dimer susceptibility (top) at low temperature. One should note from the form of the fitted function that the monomers contribute 1/3 of the spins and the dimers contribute 2/3 of the spins.

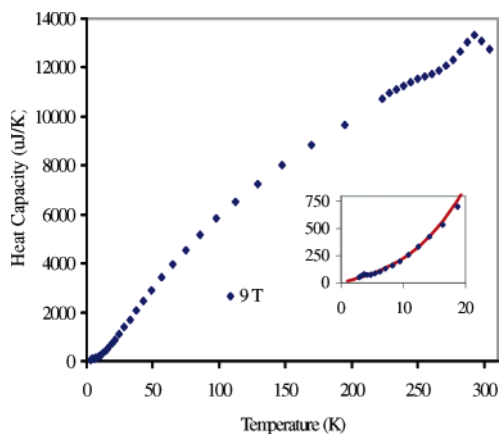
As suggested by one reviewer, magnetic susceptibility was remeasured from 4 to 400 K (Figure S8 in the Supporting Information). Measurements up to 800 K would give valuable information. If the susceptibility increases with increasing temperature at higher temperature, it would suggest the presence of a large spin gap. However, the instrument is

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(21) Sebastian, S. E.; Yin, D.; Tanedo, P.; Jorge, G. A.; Harrison, N.; Jaime, M.; Mozharivskij, Y.; Miler, G.; Krzystek, J.; Zvyagin, S. A.; Fisher, I. R. *Phys. Rev.* **2005**, *71B*, 212405/1.



**Figure 5.** Specific heat measurement for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  in zero magnetic field. Inset gives the  $C_p$  vs  $T$  curve between 2 and 20 K.

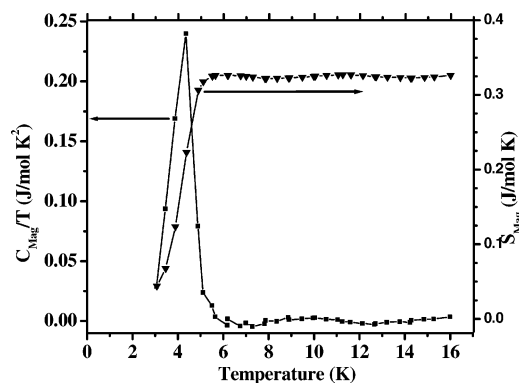


**Figure 6.** Specific heat measurement for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  in 9 T field. Inset gives the  $C_p$  vs  $T$  curve between 2 and 20 K.

limited to a maximum temperature of 400 K. Therefore, data were fit by the Curie–Weiss Law from 50 to 200 K, the dimer contribution was neglected in this temperature range, and a Curie term of  $2/3$  was obtained. The observed susceptibility likely is not due to the unpaired Cu(2) spins alone because a value of  $1/3$  would be expected in this case.

**Specific Heat.** Figure 5 shows the variation of the specific heat for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  in zero magnetic field, as a function of temperature between 2 and 300 K. The specific heat measurement for  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  shows a  $\lambda$ -type anomaly at  $\sim 4$  K, which is ascribed to magnetic impurities and/or defects of  $\text{Cu}^{2+}$  ions. Additionally, the specific heat measurement in 9 T field between 2 and 300 K shows another anomaly at 290 K, as shown in Figure 6 (the anomaly at 4 K is unaffected by the field). No clear cause for the peak at 290 K in 9 T field is evident in this model, but it has been verified that it reproduces itself. It is possible that closer inspection will reveal similar results in  $H = 0$  specific heat observations.

Figure 7 shows graphs of  $C_{\text{mag}}/T$  vs  $T$  and of  $S_{\text{mag}}$  vs  $T$  (magnetic heat capacity and magnetic entropy, respectively). The magnetic heat capacity was obtained by fitting the heat capacity data from 7 to 15 K to the form  $C_p = aT + bT^3 + cT^5$  to obtain a reasonable representation of lattice, electronic, and nuclear heat capacities combined. This representation was then extrapolated to zero temperature and subtracted pointwise from our data. The result was then divided by the



**Figure 7.** Graphs of  $C_{\text{mag}}/T$  vs  $T$  and of  $S_{\text{mag}}$  vs  $T$ .

sample temperature ( $C_{\text{mag}}/T$ ) and integrated ( $S_{\text{mag}}$ ) to yield the points on the graphs. The oscillatory behavior in these graphs is the results of the polynomial model. The magnetic entropy is 330 mJ/mol·K above 6 K. This value is far too small to reflect ordering in the monomers and/or dimers, so the peak can be ascribed to the presence of impurities.

## Conclusions

The structure of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  is built up from infinite zigzag chains of  $[\text{Cu}_3\text{O}_8]^{10-}$  units, and it is possible to view these chains as alternating dimers and monomers. From the analysis of magnetic susceptibility and heat capacity,  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  has spin-gap and Curie–Weiss behavior, and the Cu(2)–Cu(2) spin dimer is the origin of the spin gap, while the Cu(1) monomer is the origin of Curie–Weiss response.

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**Supporting Information Available:** An X-ray crystallographic file in CIF format including crystallographic details, atomic coordinates, interatomic distances and angles; calculated X-ray diffraction pattern data; observed X-ray diffraction pattern data of  $\text{Pb}_2\text{Cu}_3\text{B}_4\text{O}_{11}$  before and after melting; differential thermal analysis plot; an infrared spectrum; trimer model; remeasured SQUID data to 400 K. This material is available free of charge via the Internet at <http://pubs.acs.org>.

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